

**DUE: Friday, June 18<sup>th</sup>** Please turn in a paper copy and **SHOW YOUR WORK!**

1. Consider the function 
$$P(q) = \begin{cases} -2q & q \leq 0 \\ (q - 0.25)^2 e^{-0.36(q-0.25)^2} & 0 < q < 2 \\ 2q^3 - 10.6q^2 + 17.6q - 8.8 & q \geq 2 \end{cases}$$

Be careful! Wolfram Alpha has a hard time interpreting commands applied to this function. You may want to deal with the function one piece at a time.

(a) Find all of the critical points of  $P(q)$ .  $q =$  \_\_\_\_\_

(b) Restricting our attention to the interval  $[-2, 3]$ ...

The maximum value of  $P(q)$  is \_\_\_\_\_. This occurs when  $q =$  \_\_\_\_\_.

The minimum value of  $P(q)$  is \_\_\_\_\_. This occurs when  $q =$  \_\_\_\_\_.

2. Wendy's small business uses a moderately expensive small copier. It costs \$1,500 to purchase a new copier and she has collected the following repair cost data: The first year's repair costs were \$75 and the second year's repairs cost \$325. Model the average annual cost of the copier using a function of the form:  $A(t) = \frac{C}{t} + Rt^r$  where  $C$  is the cost of purchasing a copier and  $Rt^r$  models the repair costs.

Use the facts  $Rt^r = 75$  when  $t = 1$  and  $Rt^r = 200 \left( = \frac{75 + 325}{2} \right)$  when  $t = 2$  to find  $R$  and  $r$ .

$A(t) =$  \_\_\_\_\_

Wendy should replace the copier every \_\_\_\_\_ years and \_\_\_\_\_ months.

If she does this, her average annual cost will be \$ \_\_\_\_\_.

3. Frank has a neighborhood grocery store. One of his most popular items is 25 lbs. bags of premium rice. In fact, he sells 1000 bags each year. Each bag costs Frank \$20. He pays \$150 every time he gets the rice delivered and his inventory costs are \$1.25 per bag per year (base inventory on average inventory with the standard assumptions).

(a)  $C(x) =$  \_\_\_\_\_

Frank's **ideal** EOQ is \_\_\_\_\_. His **ideal** minimum annual cost is \_\_\_\_\_.

- (b) Suppose that Frank gets a discount if he places an order of 400 or more bags of rice. For orders of 400 or more, he gets the bags for \$17.50. However, his shipping costs increase to \$200 for a large shipment and he found that his inventory cost rise to \$2.50 a bag.

$$C(x) = \begin{cases}$$

In this case, Frank's **ideal** EOQ is \_\_\_\_\_. His **ideal** minimum annual cost is \_\_\_\_\_.

- (c) Are the solutions from parts (a) or (b) **practical solutions**? Explain.