

Please turn in a paper copy and **SHOW YOUR WORK!**

1. Consider the function  $f(x) = \begin{cases} -0.2x^2 + x + 3 & x \leq -1 \\ (x - 0.2)^2 e^{-0.3(x-0.2)^2} & -1 < x < 2 \\ 2x^3 - 10.6x^2 + 18x - 9 & x \geq 2 \end{cases}$

Be careful! Wolfram Alpha may have trouble with this function. You might want to deal with it one piece at a time.

(a) Find all of the critical points of  $f(x)$ .  $x =$  \_\_\_\_\_(b) Restricting our attention to the interval  $[-2, 3]$ ...The maximum value of  $f(x)$  is \_\_\_\_\_. This occurs when  $x =$  \_\_\_\_\_.The minimum value of  $f(x)$  is \_\_\_\_\_. This occurs when  $x =$  \_\_\_\_\_.

2. Green Villa Resort (located in Greenville, NC) uses golf carts to transport their guests around the grounds. Their carts cost \$2,000. They have noticed that a cart typically requires \$100 of repairs and maintenance during its first year of operation, then \$360 during its second year, and then \$660 during its third year.

Use Excel to find a power model for the **average** annual repair costs. Then model the average annual cost of operating a golf cart using a function of the form:  $A(t) = \frac{C}{t} + Rt^r$  where  $C$  is the cost of purchasing the cart and  $Rt^r$  models the repair costs.

$$A(t) = \underline{\hspace{10cm}}$$

When  $t =$  \_\_\_\_\_,  $A(t)$  is minimized. [Keep 5 decimal places.]

Green Villa should replace its golf carts every \_\_\_\_\_ years and \_\_\_\_\_ months.  
[Round up to the next whole month.]

If they do this, their average annual cost (per cart) should be \$ \_\_\_\_\_.

3. Jonas manages an office which uses a lot of paper. He can get paper for \$3 a ream and has found that his average storage cost is \$0.05 per ream per year (base inventory costs on average inventory making all of the standard assumptions). Finally, Jonas pays \$30 every time he places an order. Let  $C(x)$  be his annual cost function (for paper).

(a) If Jonas needs 1,000 reams each year,  $C(x) =$  \_\_\_\_\_His **ideal** EOQ is \_\_\_\_\_ and his **ideal** minimum annual cost is \_\_\_\_\_.(b) If Jonas needs 10,000 reams each year,  $C(x) =$  \_\_\_\_\_His **ideal** EOQ is \_\_\_\_\_ and his **ideal** minimum annual cost is \_\_\_\_\_.

- (c) Suppose that Jonas needs 5,000 reams each year. In addition, he found out that he gets a discount if he places a large order. For orders of 1,000 reams or more, he pays \$2.75 per ream. However, the paper company makes large deliveries in their "big truck", so the shipping cost jumps to \$200 and Jonas also figured that his inventory costs jump up to \$0.15 per ream (based on average inventory).

$$C(x) = \begin{cases}$$

His **ideal** EOQ is \_\_\_\_\_. His **ideal** minimum annual cost is \_\_\_\_\_.