

Use Maple to answer the following questions. **Please turn in a print out of your Maple work — including the requested graphs.**

$$I = \int_0^2 \sin(x^2) dx \quad \text{and} \quad f(x) = \sin(x^2)$$

1. Plot  $f(x)$  where  $0 \leq x \leq 2$ .
2. Use Maple's "int" and "evalf" commands to approximate  $I$ .
3. Make Maple output plots illustrating the following approximations of  $I$ :
  - (a)  $L_5$
  - (b)  $T_5$
  - (c)  $S_{10}$
4. Make Maple output the corresponding summations for problem #3's approximations.
5. Finally, make Maple output the corresponding values for problem #3's approximations.
6. Determine the absolute maximum and absolute minimum of  $f'(x)$  on the interval  $[0, 2]$ .
7. Using the error bound given in the textbook (Theorem 3 in 6.2), find  $n$  so that  $|I - L_n| \leq 0.005$ .
8. Using the  $n$  you found in the last part, compute  $L_n$  and verify that  $|I - L_n| \leq 0.005$ .
9. Determine the absolute maximum and absolute minimum of  $f''(x)$  on the interval  $[0, 2]$ .
10. Using the error bound given in the textbook (Theorem 3 in 6.2), find  $n$  so that  $|I - M_n| \leq 0.005$ .
11. Using the  $n$  you found in the last part, compute  $M_n$  and verify that  $|I - M_n| \leq 0.005$ .